

# Dynamic Modeling and Analysis of DFIG based Wind Turbine for Variable Wind Speed

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## Abstract

Over the last ten years, the global wind energy capacity has increased rapidly and became the fastest developing renewable energy technology. But unbalances in wind energy are highly impacting the energy conversion and this problem can be overcome by using variable speed wind turbines. Doubly Fed Induction Generator (DFIG) based Wind Energy Conversion Systems (WECS) are gaining tremendous attention nowadays. In this paper the mathematical modeling of wind turbine is simulated in MATLAB and the results are analyzed for both fixed and variable wind speed. Also dynamic modeling of DFIG has been simulated using MATLAB/SIMULINK and the dynamic behavior of DFIG driven by wind turbine is simulated for variable wind speed.

**Keywords:** WindTurbine, Doubly-fed induction generator, Wind Energy Conversion System.

## I. INTRODUCTION

In the recent years, renewable energy systems have attracted the great interest because conventional sources of energy are limited and a number of problems associated with their use, like environment pollution, large grid requirements etc. Government of the whole world is forced for the alternative energy sources such as wind power, solar energy and small hydro-electric power [1]. Among the above given choices, wind energy is a realistic way of harnessing the natural energy. Wind energy has been intensively investigated in recent years in many different countries, which resulted in several different configurations like fixed speed system with a SCIG, the variable speed system with permanent magnet synchronous generator (PMSG) and the variable speed system with a DFIG to improve the efficiency, power rating, cost benefit effectiveness etc [2].

Wind is highly variable in nature, so variable speed Doubly Fed Induction Generator based WECS offers many advantages compared to the fixed speed squirrel cage induction generators, such as reduced converter rating, cost, losses in result of that an improved efficiency, easy implementation of power factor correction, variable speed operation and four quadrants active and reactive power control capabilities. Due to variable speed operation, total energy output is much more in case of DFIG-based WECS, so capacity utilization factor is improved and cost of per unit energy is reduced [3].

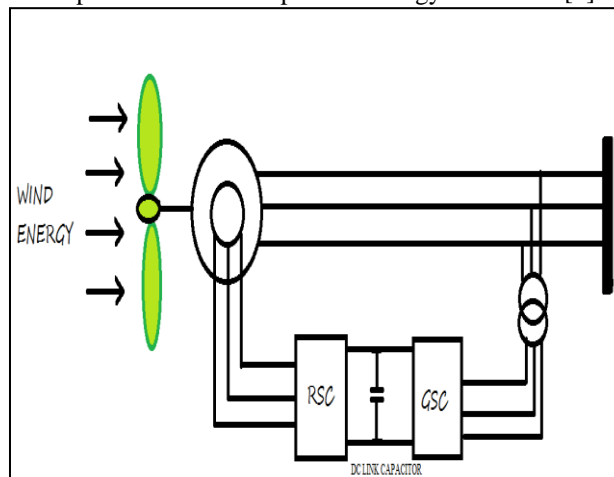


Fig. 1: DFIG based WECS

A DFIG based wind energy conversion system is shown in Fig.1. Here stator of the DFIG is directly connected to the grid and the rotor is connected to the grid via a back to back PWM Voltage Source Converter (VSC). There are a lot of advantages of using DFIG in wind energy conversion system. The main advantage is the ability of generator to supply power both at lagging and leading power factors. The other advantage is the control of the rotor voltages and currents enables the induction machine to remain synchronized with the grid while the wind turbine speed varies. The main reason for the popularity of the doubly fed

wind induction generators is their ability to supply power at constant voltage and frequency while the rotor speed varies. Hence DFIG became more popular in wind power applications. Again controlling the DFIG from the rotor side makes the control process more cost effective as the rotor converters have to deal with comparatively less power when connected at the rotor side than when connected at the stator side.

In this paper a mathematical modeling of wind turbine has been simulated using MATLAB/SIMULINK and the results are analyzed for fixed and variable wind speed. Also modeling and simulation of DFIG is done in MATLAB/SIMULINK platform and the dynamic behaviour of DFIG driven by wind turbine is simulated for variable wind speed.

## II. WIND TURBINE MODELING

The possible amount of wind power, which can be harvested by a wind turbine, is limited theoretically to 58% of total power content of the wind, considering Betz limit [4-5]. The wind turbine power coefficient is typically lower than 0.45. The generalized mechanical equation of the wind turbine is given as

$$J_s \frac{dw_r}{dt} + B_s wr = T_m - T_e \quad (1)$$

In which,  $J_s$  is total inertia of the shaft,  $B_s$  is friction coefficient,  $T_m$  is the torque with wind origin and  $T_e$  is the electromagnetic torque produced by the generator. The generated torque is given by

$$T_m = \frac{P_m}{\omega_r} \quad (2)$$

$P_m$  is the amount of mechanical power generated from the wind turbine.

$$P_m = 0.5 \rho A C_p (\lambda, \beta) V^3 \quad (3)$$

$\rho$  is the air density,  $A$  is the swept area,  $C_p$  is the coefficient of performance,  $\lambda$  is the Tip speed ratio.

$$\lambda = \frac{\omega_m R}{V^3} \quad (4)$$

There are a number of approximations available for Coefficient of Performance ( $C_p$ ).

$$C_p = 0.5176 \left[ \frac{116}{\lambda_i} - 0.4\beta - 5 \right] e^{-\lambda_i} + 0.006795\lambda \quad (5)$$

The  $C_p$  for constant wind is 0.48. Fig.2 shows the SIMULINK model of wind turbine.

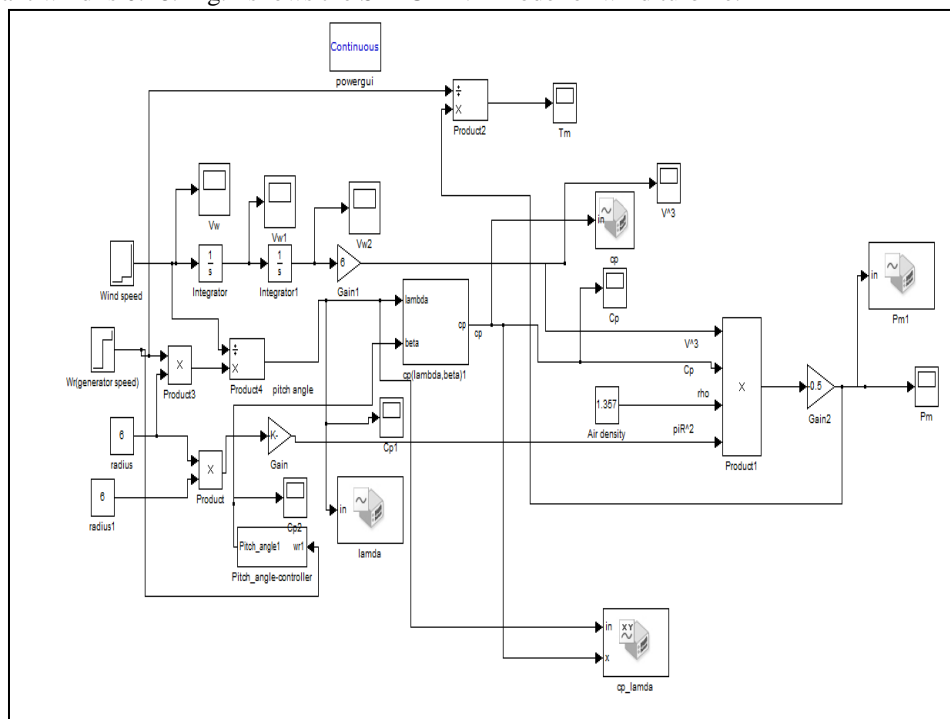


Fig. 2: Simulink model of Wind Turbine

### III. MODELING AND ANALYSIS OF THE DOUBLY-FED INDUCTION GENERATOR

A doubly-fed induction generator is as a standard wound rotor induction generator with its stator windings directly connected to the power grid and rotor connected to the power grid through a frequency converter [6-7]. The operation of DFIG can be analyzed using the classic theory of rotating fields and well known d-q model, as well as both three-to-two and two-to-three axes transformations.

The dynamic modeling of doubly-fed induction generator in synchronously rotating reference frame de–qe involves the following equations.

$$V_{sd} = R_s I_{sd} + \frac{d\phi_{sd}}{dt} - \omega_s \phi_{sq} \quad (6)$$

$$V_{sq} = R_s I_{sq} + \frac{d\phi_{sq}}{dt} - \omega_s \phi_{sd} \quad (7)$$

$$V_{rd} = R_r I_{rd} + \frac{d\phi_{rd}}{dt} - \omega_r \phi_{rq} \quad (8)$$

$$V_{rq} = R_r I_{rq} + \frac{d\phi_{rq}}{dt} - \omega_r \phi_{rd} \quad (9)$$

The stator and rotor fluxes can be expressed as

$$\phi_{sd} = L_s I_{sd} + M I_{rd} \quad (10)$$

$$\phi_{sq} = L_s I_{sq} + M I_{rq} \quad (11)$$

$$\phi_{rd} = L_r I_{rd} + M I_{sd} \quad (12)$$

$$\phi_{rq} = L_r I_{rq} + M I_{sq} \quad (13)$$

The electromagnetic torque is expressed as

$$T_{em} = pM(I_{rd}I_{sq} - I_{rq}I_{sd}) \quad (14)$$

The active and reactive power taken by the machine can be represented by the following equations.

$$P_s = \frac{3}{2}(V_{ds}I_{ds} + V_{qs}I_{qs}) \quad (15)$$

$$Q_s = \frac{3}{2}(V_{ds}I_{qs} - V_{qs}I_{ds}) \quad (16)$$

Where  $d$  and  $q$  subscripts stand for the  $d$ -axis and  $q$ -axis components,  $r$  and  $s$  subscripts stand for rotor and stator,  $V$  stands for the constant grid voltage  $\phi$  stands for flux,  $R$  stands for resistance,  $I$  stands for current,  $\omega$  stands for the utility frequency,  $p$  stands for the number of pole pairs,  $\omega_r$  stands for the rotational speed of the generator rotor,

$$V_{qr} = R_r i_{qr} + \sigma L_r \frac{di_{qr}}{dt} - \omega_{sl}(\sigma L_r i_{dr} + L_o i_{ms}) \quad (17)$$

### IV. SIMULATION RESULTS AND DISCUSSION

A 30kW wind turbine is simulated using MATLAB and the results are analyzed for fixed and variable wind speed in per unit basis. Fig.3 shows the mechanical torque generated for constant wind speed of 12m/s and Fig.4 shows the mechanical torque generated for variable wind speed. In order to analyze the performance of the wind turbine wind speed is varied at 0, 3, 5 and 7seconds and the corresponding mechanical torque generated is shown in Fig.4.

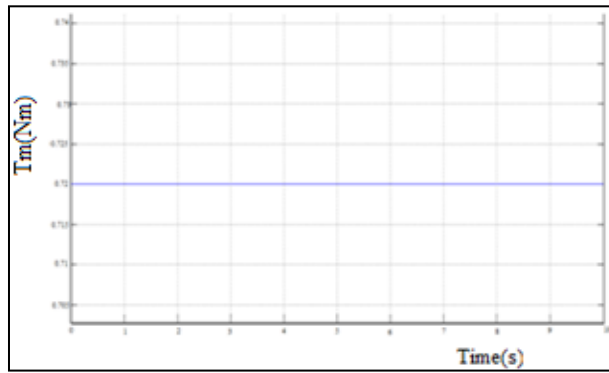


Fig.3  $T_m$  For Constant Wind Speed

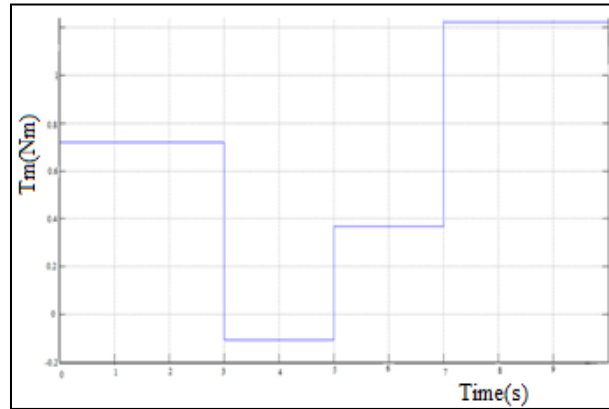


Fig. 4:  $T_m$  for Variable Wind Speed

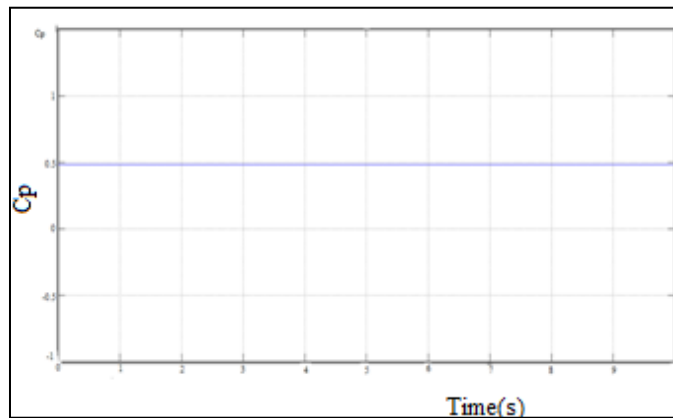


Fig. 5:  $C_p$  for Constant Wind Speed

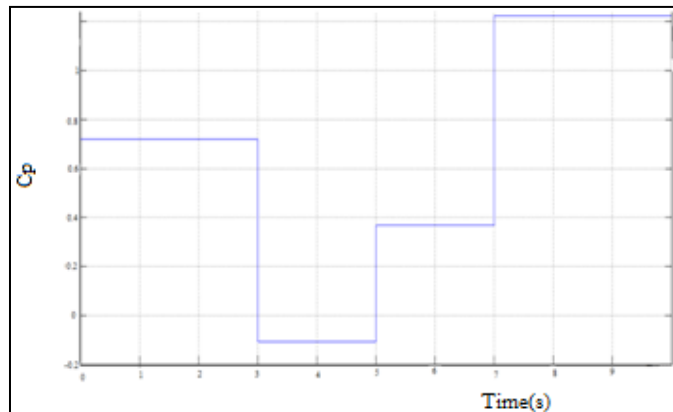


Fig. 6:  $C_p$  for Variable Wind Speed

Fig.5 shows the coefficient of performance ( $C_p$ ) for constant wind speed in per unit and Fig.6 shows the  $C_p$  for variable wind speed. The wind speed is varied at 0, 3, 5 and 7 seconds.

Fig.7 to Fig.14 shows the simulation results of Doubly Fed Induction Generator driven by wind turbine for variable wind speed. The DFIG based wind turbine is simulated using MATLAB/Simulink. The stator of the DFIG is having three phase supply. Fig.7 shows the stator voltage.

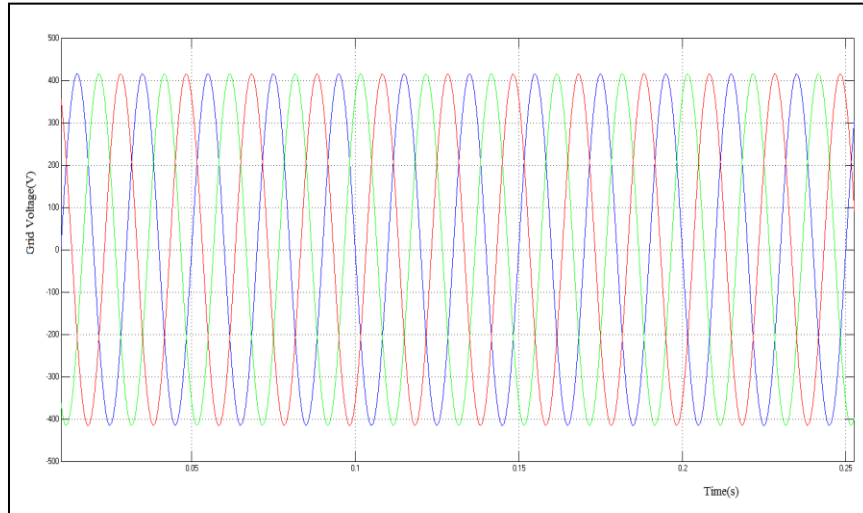


Fig. 7: Stator Voltage

The response of the DFIG system is simulated for the case of step changes in the wind speed as shown in Fig.8. The variation of wind speed at 0, 0.5 and 1 sec is shown in Fig.8. From 0 to 0.5 wind speed is 4m/s, from 0.5 to 1 it is 8m/s and beyond 1 it is 10m/s.

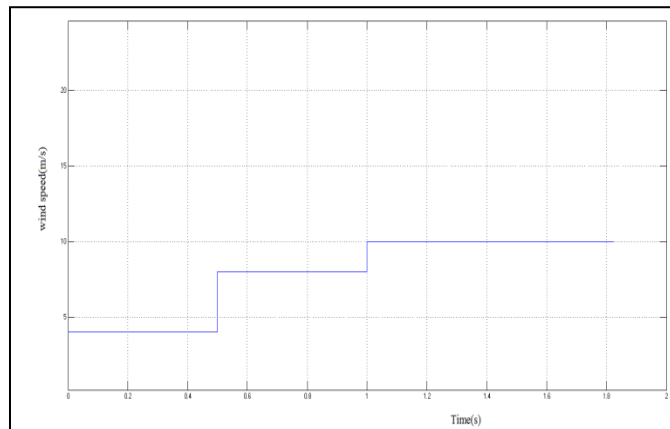


Fig. 8: Variable Wind Speed

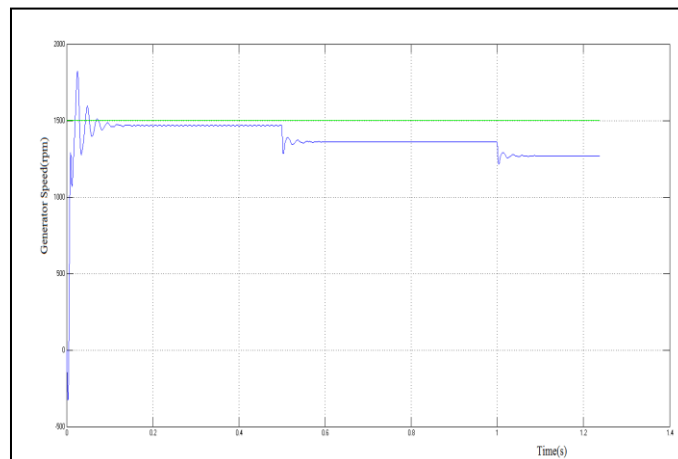


Fig. 9: Generator Speed

After the cut in speed the turbine starts generating power. When the wind speed increases the generator speed also increases [19-20]. When the wind speed is less than the rated speed rotor rotates at a speed less than the synchronous speed i.e. sub synchronous generating mode.

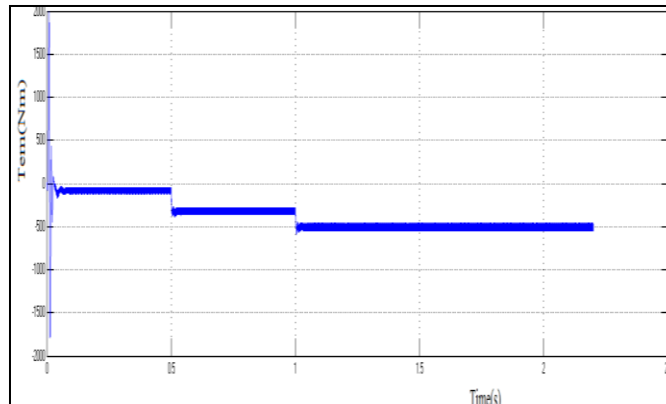


Fig. 10: Electromagnetic Torque

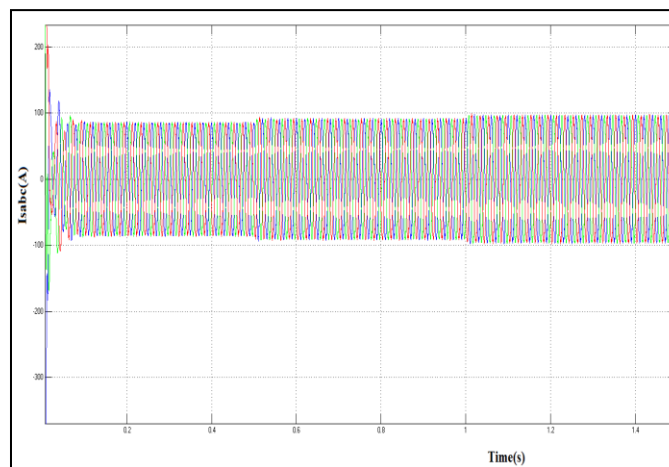


Fig. 11: Stator Current

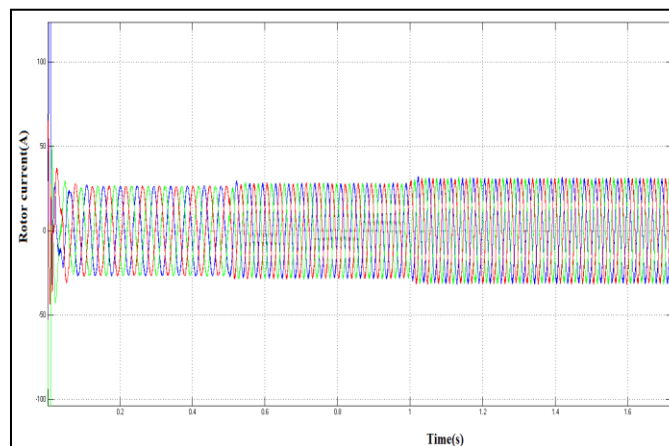


Fig. 12: Rotor Current

Fig.9 shows the sub synchronous generating mode of DFIG for variable wind speed. Fig.10 shows that when wind speed increases the torque increases and as it is a generator the torque is negative.

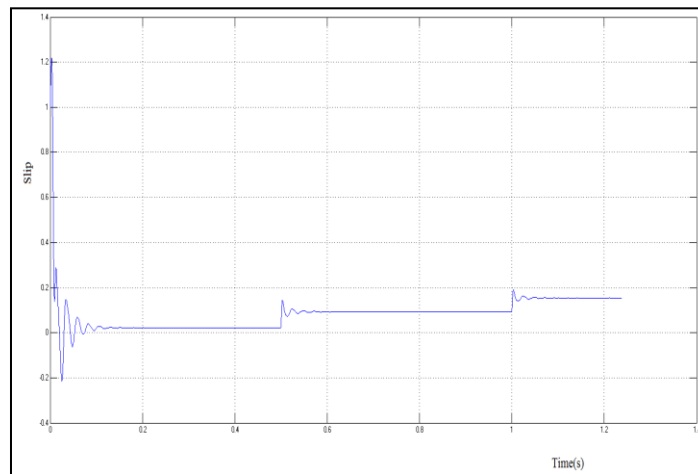


Fig. 13: Slip

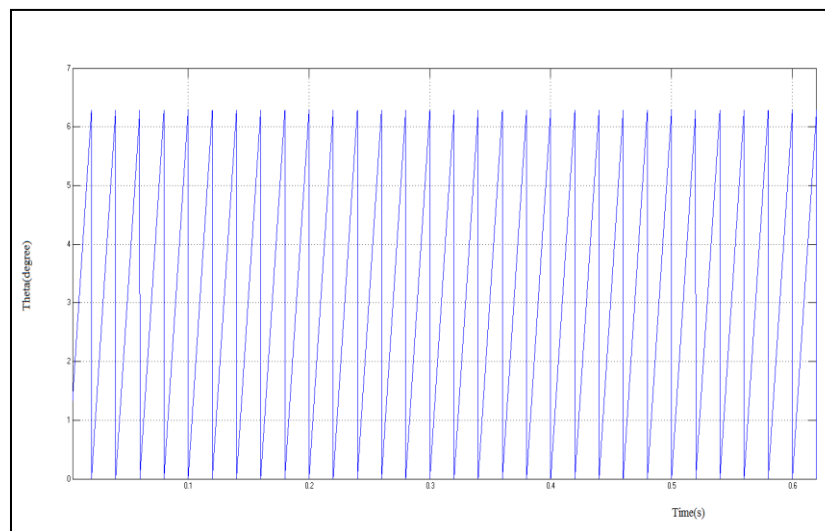


Fig. 14: Rotor Angle Theta

As the wind speed increases stator current and rotor current increases. The simulation results are shown in Fig.11 and Fig.12. Also when the speed of the generator rotor is less than the synchronous speed, the corresponding slip will be positive as shown in Fig.13. The rotor angle theta in electrical degrees is shown in Fig.14.

## V. CONCLUSION

In this paper mathematical modeling of wind turbine has been simulated using MATLAB and the results are analyzed for both fixed and variable wind speed. Also the dynamic modeling of DFIG has been simulated and the results are analyzed for variable wind speed. The results shows that the variation of wind speed induces variation in the performance of the machine.

## APPENDIX

Table – 1  
Machine Details

Parameter	Rated Values
Power(kW)	30
Voltage(V)	415
Current(A)	100
No of poles	4
Frequency(Hz)	50
Speed(rpm)	1500
Torque(Nm)	191

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